

21 **Abstract**

22 This study investigates the seasonal phase-locking of El Niño peaks using the model of Sun
23 (1997) that well simulates various characteristics of ENSO. Our findings reveal that when the
24 dynamical coupling strength between the atmosphere and ocean in the model varies
25 seasonally, as observed, El Niño events tend to peak during boreal winter. The extent of this
26 phase-locking is influenced by the amplitude of the coupling strength seasonal cycle through
27 the nonlinear frequency locking. In observations, El Niño peaks in winter because the coupling
28 strength is highest in October and lowest in April. The time lag between the peak coupling
29 strength and the peak El Niño magnitude is related to the amplitude of the seasonal cycle in the
30 coupling strength. Furthermore, we found the higher coupling strength in the seasonal cycle
31 may correspond to a higher ENSO growth rate by calculating the seasonal cycle of the model
32 equilibriums.

33 **Plain Language Summary**

34 Observations show that El Niño events, which have significant global impacts, tend to reach
35 their peak intensity during the Northern Hemisphere winter, from November to January. This
36 phenomenon is known as the seasonal phase-locking of El Niño. In this study, we use a
37 nonlinear theoretical model to explore the causes for this phase-locking. Our findings reveal
38 that the coupling strength between the ocean and atmosphere in the tropical Pacific is highest
39 in fall and lowest in spring, which causes El Niño events to peak in winter. This research is
40 important for better understanding and simulating the seasonal phase-locking of El Niño.

41 **1 Introduction**

42 The El Niño–Southern Oscillation (ENSO) is the dominant mode of interannual variability in the
43 tropical Pacific with global impacts (Cheung et al., 2021; Jian et al., 2021; Leung & Zhou, 2016;
44 Tu et al., 2022; Wang et al., 2014; Zhang et al., 2022). A key feature of El Niño is its boreal
45 winter peak phase-locking to November–January (Hirst, 1986; Philander et al., 1984).

46 However, the governing mechanism remains unclear.

47 The seasonal cycle in ocean–atmosphere coupling strength is proposed to be a critical factor in
48 El Niño peak phase-locking (Galanti & Tziperman, 2000; Timmermann et al., 2003; Tziperman et
49 al., 1998). Galanti & Tziperman (2000) and Tziperman et al. (1998) incorporated the coupling
50 strength (the linear regression coefficient of the equatorial central Pacific zonal wind response
51 to the Niño-3 sea surface temperature anomalies (SSTA)) seasonal cycle with summer maxima
52 and winter minima into the delayed oscillator mechanism and showed that the seasonally
53 varying amplification of the oceanic Rossby and Kelvin waves by the coupling strength forces El
54 Niño events to peak in boreal winter when this amplification is minimum. However, the
55 seasonal cycle is calculated from the model of Zebiak and Cane (1987) and is inconsistent with
56 observations. Timmermann et al. (2003) incorporated seasonally varying coupling strength of
57 similar definition into the nonlinear theoretical model which is also used in this study. However,
58 their research focused on the ENSO decadal variability and did not address the issue of the
59 seasonal phase-locking. Therefore, the real role of coupling strength in seasonal phase-locking
60 remains unsettled.

61 Within the recharge oscillator framework, studies (Chen & Jin, 2020, 2022; Lu & Liu, 2019; Stein
 62 et al., 2010, 2014; Zheng et al., 2024) attribute phase-locking to seasonal variations in ENSO
 63 growth rates, with autumn maxima/spring minima, thus forcing El Niño to peak in boreal
 64 winter. The declining growth rate from autumn to spring further contributes to the spring
 65 persistence barrier of ENSO (Jin et al., 2019). While researches have not reached a consensus
 66 on the primary dynamical drivers of the seasonally varying growth rate, the atmospheric
 67 thermal damping coefficient is widely recognized to play an important role (Chen & Jin, 2022;
 68 Jin et al., 2019). Thus, the damping coefficient also may be a critical factor in the phase-locking.
 69 Yu et al. (2024) utilized the model of Sun (1997) (used in this work) to investigate the roles of
 70 observational seasonal cycles of damping coefficient and dynamical coupling between zonal SST
 71 gradients and upwelling in the eastern Pacific in ENSO spring prediction barrier from the
 72 perspective of ENSO's chaotic characteristics. This work has provided new insights to the
 73 investigation on the role of damping coefficient in the phase-locking.

74 Another mechanism proposed for the phase-locking is the nonlinear frequency locking of ENSO
 75 to the seasonal cycle (Jin et al., 1994, 1996; Stein et al., 2014). The phase-locking originates in
 76 frequency-locked oscillations with ENSO frequency locked to a rational multiple of the annual
 77 cycle under external annual forcing. However, it is unclear which factor dominates phase-
 78 locking and why El Niño peaks are locked in boreal winter.

79 This research uses the ENSO model of Sun (1997) to investigate the phase-locking. The model is
 80 simple to enable sensitivity experiments on parameters and captures key physical processes
 81 associated with ENSO. We investigate the roles of the coupling strength and the atmospheric
 82 thermal damping coefficient in the phase-locking, and part I shows the results of coupling
 83 strength. The seasonal cycle is calculated from different datasets and incorporated into the
 84 model to analyze its role in the phase-locking. Amplitude/phase sensitivity experiments of the
 85 seasonal cycle are conducted to analyze factors determining the strength and peak-time of
 86 phase-locking, as well as the phase-locking mechanism. The linkage between seasonal cycles of
 87 coupling strength and ENSO growth rate is discussed. The role of atmospheric thermal damping
 88 will be in Part II.

89 **2 Methods and Data**

90 2.1 The model of Sun (1997) with seasonal cycle

91 Equations 1-6 show the original model equations, and Equation 7 shows the introduced
 92 seasonal cycle.

$$93 \quad \frac{dT_1}{dt} = c(T_e - T_1) + sq(T_2 - T_1) \quad (1)$$

$$94 \quad \frac{dT_2}{dt} = c(T_e - T_2) + q(T_{sub} - T_2) \quad (2)$$

$$95 \quad q = \frac{\alpha}{a}(T_1 - T_2) \quad (3)$$

$$96 \quad T_{sub}(h'_2) = T_e - \frac{T_e - T_b}{2} \left[1 - \tanh\left(\frac{h'_2 - H_1 + z_0}{H^*}\right) \right] \quad (4)$$

$$97 \quad \frac{1}{r} \frac{dh'_1}{dt} = -h'_1 + \frac{H_1}{2H_2} H \frac{\alpha}{b^2} (T_1 - T_2) \quad (5)$$

$$98 \quad h'_2 - h'_1 = -\frac{H_1}{H_2} H \frac{\alpha}{b^2} (T_1 - T_2) \quad (6)$$

$$99 \quad \alpha = \alpha_0 (1 + \Delta \sin(\omega_y t + \varphi)) \quad (7)$$

100 Equations 1-2 are forecast equations for the tropical Pacific SST. T_1 and T_2 respectively
 101 represent SST in the Western and Eastern Pacific (WP and EP). T_e is the radiative-convective
 102 equilibrium temperature of the tropical Pacific. Parameter c is the atmospheric thermal
 103 damping coefficient. In Equation 3, q measures the upwelling strength, and α is the dynamical
 104 ocean-atmosphere coupling strength and measures the sensitivity of wind stress to changes in
 105 zonal SST gradients. Surface wind stress is assumed to be proportional to the zonal SST
 106 gradients and the ocean currents strength is proportional to the surface wind stress (Sun & Liu,
 107 1996). Subsurface temperature T_{sub} is a function of the thermocline depth (Equation 4); h'_1 and
 108 h'_2 are respectively the deviations of WP and EP thermocline depth from its reference depth.
 109 The thermocline depths are governed by Equations 5 and 6, which follow Jin (1996). Detailed
 110 descriptions and definitions of the model variables and parameters are in the Supporting
 111 Information Text S1 and Table S1.

112 For the coupling strength seasonal cycle (Equation 7), we use the sine function to approximate
 113 the observational seasonal cycle; Δ is the amplitude of the seasonal cycle relative to/divided by
 114 the annual mean α_0 ; ω_y is the frequency of the seasonal cycle; φ is the phase determining the
 115 months of the maximum/minimum coupling strengths. The seasonal variation of coupling
 116 strength influences the system in two ways: one is the zonal SST gradients-zonal wind stress-
 117 ocean currents positive feedback (Equation 3). The other is the role of wind stress in
 118 modulating thermocline depth (Equations 5-6) (Philander, 1989). The annual mean state is set
 119 as: $T_e=31^\circ\text{C}$, $T_b=17.3^\circ\text{C}$, $1/c=150$ days, $1/r=300$ days, $H^*=65$ m, $H_1=50$ m, $H_2=150$ m, $z_0=75$ m,
 120 $\alpha_0/a=3*10^{-8} \text{K}^{-1}\text{s}^{-1}$, $H_1H\alpha_0/H_2b^2=23 \text{mK}^{-1}$, the same as Figure 5 in Liang et al. (2012). For the
 121 seasonal cycle, $\omega_y=2\pi/365 \text{day}^{-1}$, we will show that $\Delta\approx 0.5$, $\varphi=335\pi/365$, meaning the
 122 maximum/minimum coupling strength in October/April. In each experiment, the model is run
 123 for 3000 years with 1.5-day time step. We calculate the monthly mean of results from the latter
 124 2000 years and calculate the interannual anomalies by removing the climatology in each month.
 125 El Niño events are defined as occurring when EP SST (T_2) anomalies exceed +1.0 standard
 126 deviation.

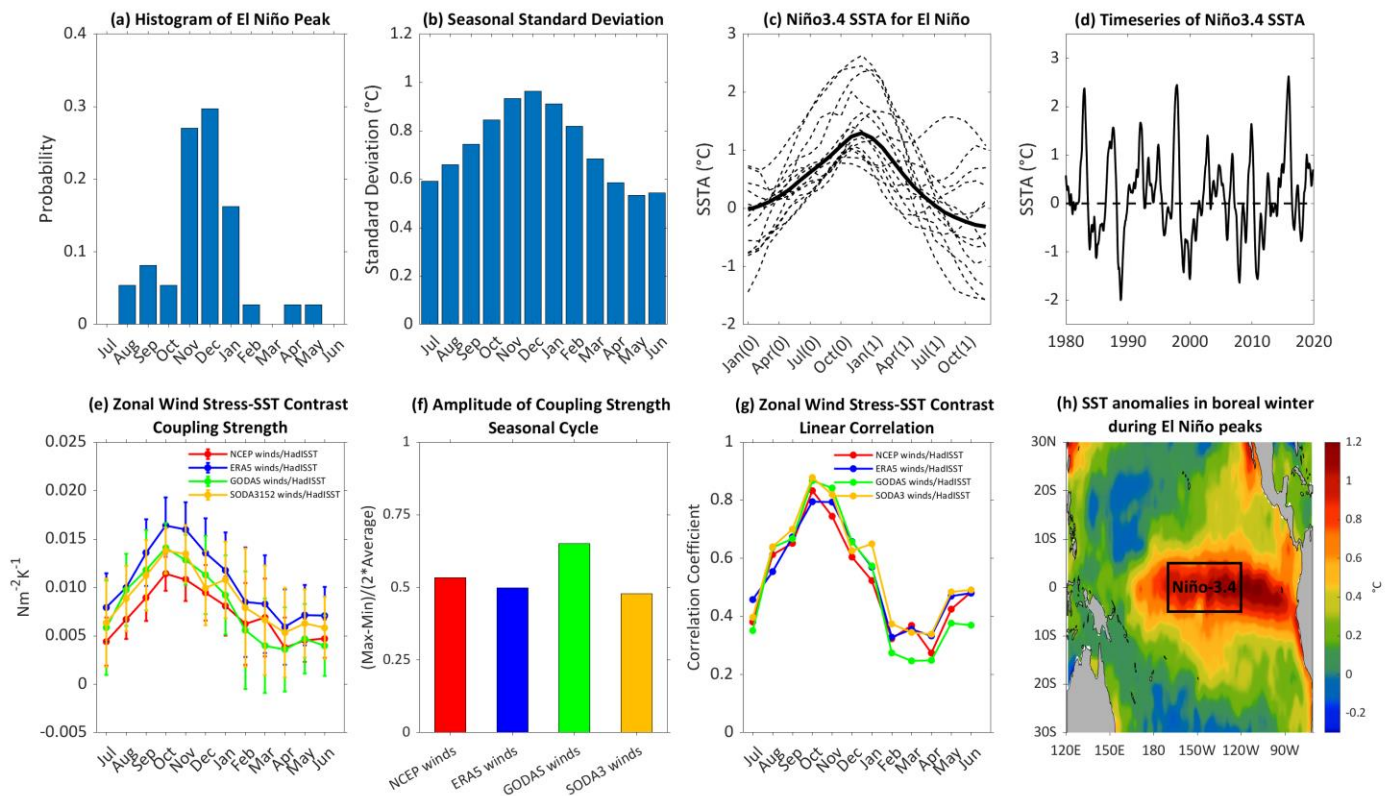
127 **2.2 Observations**

128 The monthly SST is from the Hadley Centre Global Sea Ice and Sea Surface Temperature dataset
 129 (HadISST; Rayner et al., 2003) during 1870-2023. The phase-locking in the Niño-3.4 region (5°S–
 130 5°N, 190°-240°E) in the observations is analyzed. An El Niño event is defined as occurring when
 131 the 3-month running averaged SSTA index exceeds +1.0 standard deviation. The anomalies are
 132 based on the climatology of the dataset period.

133 The zonal wind stress from four datasets are used: 1) NCEP-NCAR Reanalysis 1 (Kalnay et al.,
 134 1996) during 1948-2023; 2) The fifth-generation ECMWF atmospheric reanalysis of the global
 135 climate (ERA5, Hersbach et al., 2020) during 1948-2023; 3) the Global Ocean Data Assimilation
 136 System (GODAS; Behringer et al., 1998) during 1980-2023; and 4) the Simple Ocean Data
 137 Assimilation (SODA) 3.15.2 dataset (Carton et al., 2018) during 1980-2023. When calculating the
 138 coupling strength for a particular month, we linearly regress the monthly mean interannual
 139 anomalies of the zonal wind stress in the central equatorial Pacific (5°S-5°N, 160°-200°E) to the
 140 corresponding variations in the equatorial zonal SST contrast calculated from the HadISST
 141 dataset (Sun, 2003; Sun et al., 2004). The contrast is defined as the area-averaged SST
 142 difference between (5°S–5°N, 130°E–180°) and (5°S–5°N, 230°-280°E).

143 **3 Results**

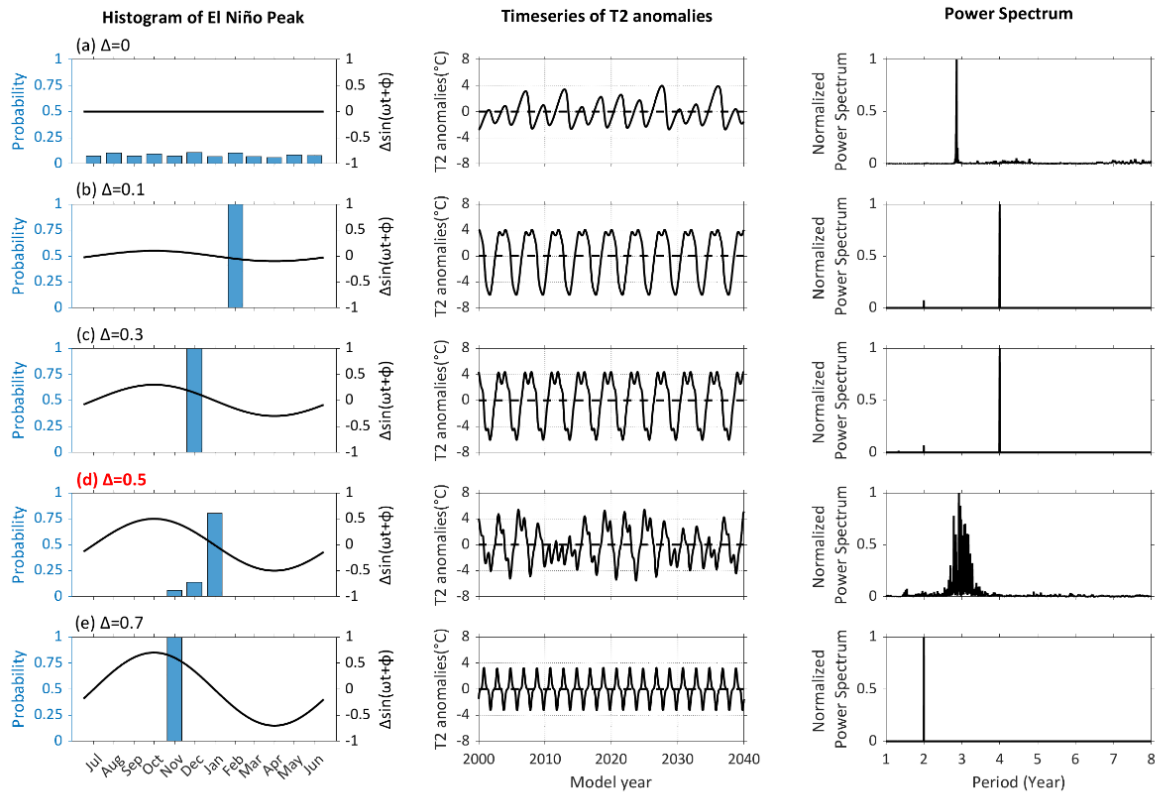
144 **3.1 Observed phase-locking of El Niño peaks and seasonal cycle in ocean-atmosphere coupling**
 145 **strength**



147 **Figure 1.** (a) Histogram of El Niño peak probabilities in 12 months (37 events). (b) Seasonal standard deviation of
148 Niño-3.4 SSTA index. (c) Two-year segments of Niño-3.4 SSTA index for El Niño. (thick curve: composite mean, thin
149 dashed curves: individual El Niño events over the past 50 years, Year(0): the former year, Year(1): the latter year).
150 (d) A portion of the Niño-3.4 SSTA index timeseries (1980-2020). (e) Seasonal cycle of zonal wind stress-SST
151 contrast coupling strength. Vertical error bars represent 95% confidence intervals for the linear regression
152 coefficient (coupling strength). Colored curves represent results calculated from different datasets. (f) Amplitude
153 of the coupling strength seasonal cycle (defined as half the maximum-minimum difference divided by the average).
154 (g) Seasonal cycle of the linear correlation coefficients between the zonal wind stress and zonal SST contrast
155 anomalies. (h) Tropical Pacific SSTA in boreal winter (Nov-Jan) during El Niño peaks (averaged for events over the
156 past 50 years).

157
158 Figures 1a-1d illustrate the observed El Niño peak phase-locking characteristics via Niño-3.4
159 SSTA during 1870-2023. Figure 1a shows a histogram of El Niño peaks indicating that El Niño
160 events tend to peak during boreal winter (November-January). Figure 1b shows that standard
161 deviation shows a seasonal cycle with the peak in December and valley in May. Figure 1c
162 depicts the composite evolution of El Niño (thick line) around the time it peaks; The averaged
163 evolution peaks during boreal winter, which further demonstrates the phase-locking feature.
164 Figure 1d shows the Niño-3.4 SSTA index timeseries, indicating the nonlinear characteristics of
165 ENSO, such as irregularity and amplitude diversity.
166 Figures 1e-1g show the coupling strength calculated from datasets. The coupling strength
167 shows a strong annual cycle (Figure 1e). The coupling strength reaches the maximum in
168 October (boreal autumn) and decreases thereafter until it reaches the minimum in April
169 (spring). The seasonal phases are highly consistent across datasets. Figure 1f presents the
170 calculated seasonal cycle amplitude defined as $(\max - \min) / (2 * \text{mean})$. Three datasets
171 (NCEP-NCAR Reanalysis 1, ERA5, and SODA 3.15.2) show an amplitude of 0.5, while GODAS
172 dataset yields a higher value of 0.65. The coupling strength is strongest in boreal autumn and
173 weakest in spring, while El Niño events tend to peak during the intervening winter months.
174 Figure 1g shows the seasonal cycle of the zonal wind stress-zonal SST gradient correlation, with
175 the strongest/weakest correlation in October/February-April and high consistency across
176 different datasets. This suggests that in boreal spring, the weaker response of wind stress to
177 SST anomalies may be due to a lower correlation between the two. Calculation details of the
178 seasonal cycles of coupling strength and correlation coefficient are in the scatter plots for zonal
179 SST gradient and zonal wind stress anomalies in 12 months shown in Supporting Information
180 (Figure S1). Figure 1h shows the SST anomaly spatial distribution at the peak of El Niño during
181 boreal winter, with warm SST anomalies concentrated in the central and eastern equatorial
182 Pacific. The black box highlights the Niño-3.4 region.

183 3.2 Phase-locking of El Niño peaks simulated by the model with coupling strength seasonal cycle

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185

186 **Figure 2.** (left) Histograms of El Niño Peak from experiments with the increasing amplitudes of coupling strength
 187 seasonal cycle (Δ). (a) $\Delta=0$ (annual mean case), (b) $\Delta=0.1$, (c) $\Delta=0.3$, (d) $\Delta=0.5$ (red bold font, observations), (e)
 188 $\Delta=0.7$. The phase is fixed at $\phi=335\pi/365$ (maximum/minimum in October/April). (middle) and (right) are 40-yr
 189 portions and the power spectrum of T_2 anomaly timeseries from each experiment.

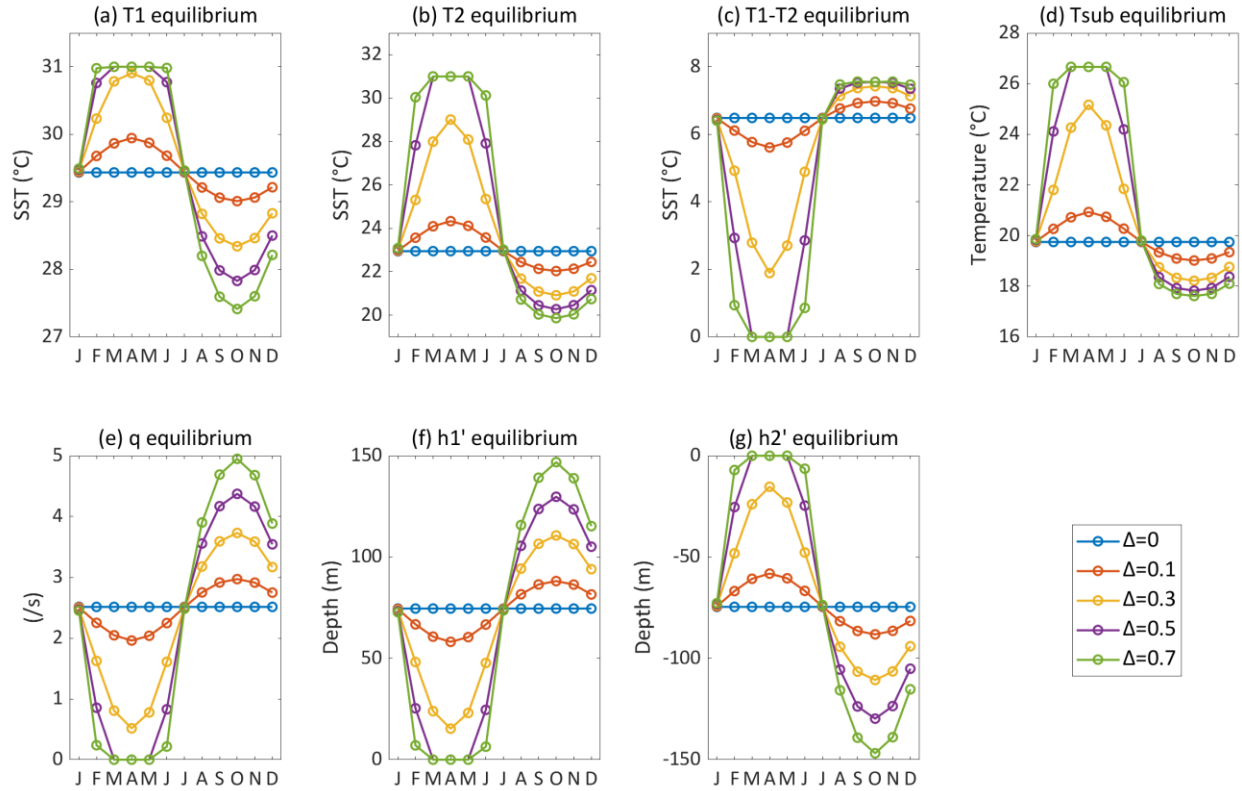
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191 Figure 2 shows the experiments where the coupling strength seasonal cycle is incorporated into
 192 the model, with its amplitude gradually increased. The maximum/minimum coupling strength is
 193 in October/April as observed. When the amplitude approaches the observed value ((d) $\Delta = 0.5$),
 194 the El Niño peaks lock to boreal winter (November-January). This demonstrates that
 195 incorporating the observed coupling strength seasonal cycle effectively simulates the phase-
 196 locking characteristics. Additionally, T_2 anomalies timeseries shows the diversity and decadal
 197 variability of ENSO amplitude, which is consistent with observations. In the frequency domain,
 198 the power spectrum displays a broadband distribution with prominent peaks at approximately
 199 3-year period. Compared to the original model((a) $\Delta=0$), the introduction of observed seasonal
 200 cycle improves the simulations in the frequency aspects.

201 Next, we examine the impacts of the seasonal cycle amplitude on the phase-locking strength.
 202 Without seasonal cycle, El Niño peaks distribute uniformly across months, indicating no phase-
 203 locking((a) $\Delta=0$). When the seasonal cycle is introduced ((b) $\Delta = 0.1$ and (c) $\Delta = 0.3$), El Niño
 204 peaks are completely locked to one single month. As the seasonal cycle amplitude increases to
 205 0.5 (d), the phase-locking weakens, with peak-time across November-January. With further

206 increases in amplitude ((e) $\Delta = 0.7$), all El Niño peaks again align within one single month. These
207 results illustrate that the phase-locking due to the nonlinear frequency locking of ENSO to the
208 seasonal cycle (Jin et al., 1994, 1996; Stein et al., 2014). Experiments (b), (c), and (e) yield
209 frequency-locked solutions with strictly periodic oscillations, where ENSO frequency is a
210 rational multiple of the seasonal cycle. In (b) and (c), the power spectrum shows the 4-year
211 ENSO period, while (e) shows the 2-year period, causing all El Niño events to peak in one month.
212 Experiment (d) represents the chaotic situation where irregular shifts between frequency-
213 locked solutions cause El Niño to peak in several consecutive months instead of locking in one
214 month. However, these shifts do not move the peaks to other seasons, all peaks remain in
215 boreal winter. When $\Delta = 0.9$, ENSO is suppressed, leaving only seasonal frequency in the forced
216 system (Chang et al., 1994). This result is in the Figure S2 in the Supporting Information.
217 These findings highlight that the amplitude of the coupling strength seasonal cycle modulates
218 the strength of phase-locking. Besides, the variation amplitude of the seasonal standard
219 deviation of T_2 increases with the seasonal cycle amplitude, further demonstrating its
220 modulating effect on phase-locking strength. Seasonal std and trajectory of the system,
221 projected onto the plan of T_2 and h_1' are in the Figure S3 in the Supporting Information.
222 Then, we discuss the influence of the seasonal cycle amplitude on the timing of El Niño phase-
223 locking. As shown in Figure 2 and Figure S3, El Niño events tend to peak within boreal winter in
224 all the experiments where the coupling strength seasonal cycle is incorporated (Experiments
225 (b)-(e)). However, as the seasonal cycle amplitude varies, the time lag between the peak in
226 coupling strength and the El Niño peak shifts, affecting the timing of phase-locking. In
227 Experiment (b), with a relatively low seasonal cycle amplitude, this lag is about four months,
228 placing the peak in February. As the seasonal amplitude increases in (c) and (d), the lag
229 shortens to 2-3 months, shifting the peak to December-January. In (e), the peak is further
230 advanced to November with an even larger seasonal amplitude.

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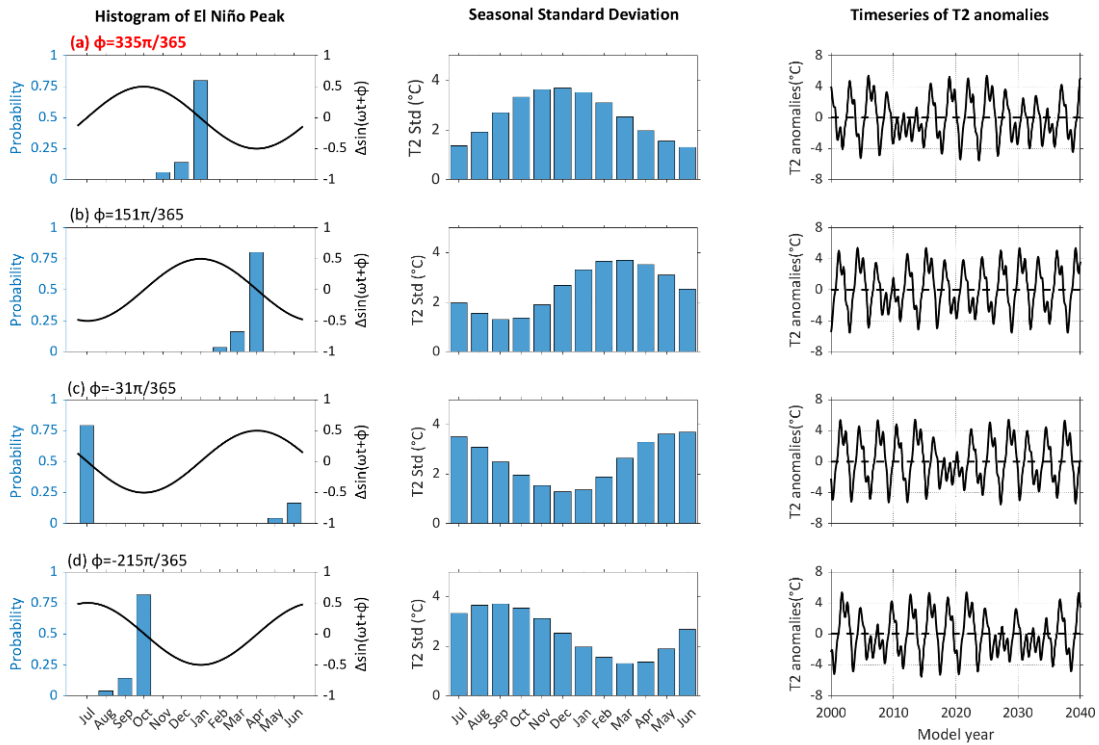
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233 **Figure 3.** Equilibrium values as a function of coupling strength across the seasonal cycle. (a) the western equatorial
 234 Pacific (WEP) SST, T_1 ; (b) the eastern equatorial Pacific (EEP) SST, T_2 ; (c) zonal SST contrast T_1-T_2 ; (d) subsurface
 235 temperature T_{sub} ; (e) upwelling q ; (f) WEP thermocline depth h_1' ; (g) EEP thermocline depth h_2' . Curves in different
 236 colors represent different seasonal cycle amplitudes. The equilibria are calculated at fixed coupling strength of
 237 each month in the seasonal cycle.

238

239 Previous studies have shown that the phase-locking of El Niño peaks is dominated by the
 240 seasonal cycle of ENSO growth rate (Chen & Jin, 2020, 2022; Stein et al., 2010, 2014). Figure 3
 241 shows equilibrium states of the model as a function of coupling strength across the seasonal
 242 cycle. It can be seen that in the boreal autumn (strong coupling strength), WEPSST (T_1) and
 243 EEPSST (T_2) get colder in Figure 3a-3b. The zonal SST contrast increases because EEPSST
 244 decreases faster in Figure 3c. The wind stress is strengthened, and the upwelling (q) is stronger
 245 in Figure 3e. More heat content accumulates in the upper layer of the WP to form a deeper
 246 thermocline depth (h_1') in Figure 3f. In the EP, the thermocline depth (h_2') is shallower (Figure
 247 3g) with colder subsurface temperature (Figure 3d). The situations in autumn may represent a
 248 higher ENSO growth rate. While in spring with the weakest coupling strength, the zonal
 249 contrast between the WP and EP becomes smaller in SST, thermocline depth (a more zonally
 250 symmetric equilibrium state) which represent a lower growth rate. Thus, introducing a seasonal
 251 cycle of coupling strength into the model may be equivalent to partially incorporating a
 252 seasonal cycle of ENSO growth rate into the recharge-discharge oscillator. The growth rate
 253 reaches maximum/minimum in autumn/spring, which is consistent with Chen & Jin (2020,
 254 2022).

255



256

257 **Figure 4.** (left) Histograms of El Niño peak from experiments with varying phases of the coupling strength seasonal
 258 cycle (ϕ). (a) $\phi=335\pi/365$ (max/min: Oct/Apr) consistent with observations. (b) $\phi=151\pi/365$ (max/min: Jan/Jul). (c)
 259 $\phi=-31\pi/365$ (max/min: April/Oct). (d) $\phi=-215\pi/365$ (max/min: Jul/Jan). Amplitude of the seasonal cycle is fixed at
 260 $\Delta=0.5$. (middle) and (right): seasonal standard deviations and 40-yr portions of the T_2 anomaly timeseries from
 261 each experiment.

262

263 Figure 4 shows the phase sensitivity experiments of the coupling strength seasonal cycle. The
 264 amplitude is fixed ($\Delta=0.5$). In experiment (a) (the phase aligns with observations), El Niño
 265 peaks lock to boreal winter with a time lag of 2-3 months between the coupling strength peak
 266 and the El Niño event peak. In the other three experiments, when the phase ϕ is shifted, the
 267 locking season of El Niño peaks shifts correspondingly, and the time lag of 2-3 months remains
 268 consistent. In Experiment (b), the maximum/minimum coupling strength is in January/July, El
 269 Niño peaks lock in March-April (boreal spring). In (c), the maximum/minimum coupling strength
 270 is in April/October, El Niño peaks lock to June-July (boreal summer). In (d), the
 271 maximum/minimum coupling strength is in July/January, El Niño peaks lock to September-
 272 October (boreal autumn).

273 These findings indicate that the phase of the seasonal cycle in coupling strength primarily
 274 determines the timing of El Niño peaks, explaining that El Niño peaks in winter because the
 275 coupling strength is highest in October and lowest in April. Additionally, the phase of the
 276 seasonal cycle does not affect the strength of phase-locking.

277 The role of atmospheric thermal damping should be investigated through the same analysis as
 278 in part I. Firstly, the seasonal cycle is calculated from datasets, the damping coefficient is
 279 defined as the absolute value of the linear regression coefficients between net surface heating

280 and SST anomalies in eastern equatorial Pacific. The seasonal cycle is incorporated into the
281 model through parameter c . Numerical experiments will be conducted to analyze the
282 contribution to the phase-locking. The analysis will be presented in the second part of this study.

283 **4 Conclusions and Discussion**

284 The peak of El Niño has an important influence on global climate (Leung & Zhou, 2016; Li &
285 Zhou, 2012; Zhang et al., 2022; Zhang et al., 2019). We use the model of Sun (1997) to study the
286 phase-locking of El Niño peaks. The seasonal cycle of ocean-atmosphere coupling strength in
287 the equatorial Pacific is calculated from datasets. Results reveal that the maximum/minimum
288 coupling strength is in October/April, with an amplitude (half the difference between the
289 maximum and minimum values relative to the mean) of approximately 0.5. Results from
290 different datasets are highly consistent. Incorporating the observed seasonal cycle of coupling
291 strength into the model well simulates the wintertime phase-locking of El Niño peaks, affirming
292 the key role of coupling strength in this phenomenon. The simulated ENSO timeseries replicates
293 the observed irregularity and decadal variability. Amplitude sensitivity experiments of the
294 seasonal cycle reveal that the strength of phase-locking is significantly influenced by seasonal
295 cycle amplitude through nonlinear frequency-locking of ENSO to the seasonal cycle. While
296 changes in the seasonal cycle amplitude do not alter the locking season, they affect the peak-
297 time by modifying the time lag between the coupling strength peak and the El Niño peak. El
298 Niño peaks occur in boreal winter because of phase of the coupling strength seasonal cycle
299 (Maximum/Minimum in October/April). Furthermore, we found the higher coupling strength in
300 the seasonal cycle may correspond to a higher ENSO growth rate by calculating the seasonal
301 cycle of the equilibrium state of the model.

302 The important role of coupling strength in the phase-locking in this work aligns with Jin et al.,
303 (2019). The coupling strength is comparable to the thermocline positive feedback in that work
304 which is one of the two factors dominating the seasonal cycle of ENSO growth rate.
305 Furthermore, the other factor is the atmospheric thermal damping rate whose influence on the
306 phase-locking will be investigated in the next part of our work.

307 However, our study has limitations. Firstly, only the seasonal cycle of coupling strength is
308 introduced. The primary influence of coupling strength on the phase-locking may be amplified
309 or weakened by other processes as shown in the linear theory (Chen & Jin, 2022; Jin et al.,
310 2020). It is better to calculate the seasonality of each parameter and investigate their
311 contributions to the phase-locking. For now, since other processes modify the influence of
312 coupling strength, we have conducted the amplitude/phase sensitivity experiments of the
313 coupling strength seasonal cycle. All the experiments show the robust phase-locking of El Niño
314 peaks. Secondly, the introduction of coupling strength in this study causes the annual cycle in
315 upwelling/zonal current to have the same phase and amplitude as the seasonal cycle in
316 coupling strength. This hypothesis is not consistent with observations. Further work needs to
317 add the coupling strength seasonal cycle to the model from different positions respectively to
318 study their contributions to seasonal phase-locking. Thirdly, when the amplitude of seasonal
319 cycle is 0.5 corresponding to the observation, the equilibrium state and the standard deviation
320 of EP SSTA show a much stronger seasonal variation than observations. For example, the T_2
321 equilibrium has the maximum/minimum value of 31°C /20°C in Apr/Oct (Figure 3b), while in
322 observations the maximum/minimum value of the climatological state of EP SST is 27.5°C/24°C.

323 This difference may be due to that the annual mean state in the study is in the self-sustained
 324 regime with ENSO amplitude close to the real world, while researches utilize observations to
 325 show that the annual mean ENSO growth rate is slightly negative/positive near zero (not
 326 consider the seasonal cycle) (Chen & Jin, 2022; Jin et al., 2020; Xie & Jin, 2018). The parameter
 327 setting of the annual mean state here is consistent with Liang et al., (2012, 2017) and the
 328 annual mean does not change the role of coupling strength in phase-locking. However, future
 329 work needs to recalculate the annual mean state from observations. Moreover, it is found that
 330 the peak month of El Niño shifts within the boreal winter when the seasonal cycle amplitude
 331 varies, the mechanism for the shift needs to be investigated in future work.

332 Acknowledgments

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335 Open Research

336 The data is accessed through Behringer, D.W. et al. (1998) for the Global Ocean Data
 337 Assimilation System (GODAS) dataset. The data from the Simple Ocean Data Assimilation (SODA)
 338 3.15.2 dataset is obtained through Carton et al. (2018). The fifth-generation ECMWF
 339 atmospheric reanalysis of the global climate (ERA5) dataset is obtained through Hersbach et al.
 340 (2020). The NCEP-NCAR Reanalysis 1 dataset is through Kalnay et al. (1996). The Hadley Centre
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